

Nottale's formula for the gravitational Planck constant  $\hbar_{gr} = Gm/v_0$  involves parameter  $v_0$  with dimensions of velocity. I have worked with the quantum interpretation of the formula but the physical origin of  $v_0$  – or equivalently the dimensionless parameter  $\beta_0 = v_0/c$  (to be used in the sequel) appearing in the formula has remained open hitherto. In this chapter a possible interpretation based on many-sheeted space-time concept, many-sheeted cosmology, and zero energy ontology (ZEO) is discussed. In ZEO the non-changing parts of zero energy states are assigned to the passive boundary of CD and  $\beta_0$  should be assigned to it.

There are two measures for the size of the system. The  $M^4$  size  $L_{M^4}$  is identifiable as the maximum of the radial  $M^4$  distance from the tip of CD associated with the center of mass of the system along the light-like geodesic at the boundary of CD. System has also size  $L_{ind}$  defined in terms of the induced metric of the space-time surface, which is space-like at the boundary of CD. One has  $L_{ind} < L_H$ . The identification  $\beta_0 = L_{M^4}/L_H$  does not allow the identification of  $L_H = L_{M^4}$ .  $L_H$  would however naturally corresponds to the size of the magnetic body of the system in turn identifiable as the size of CD.

One can deduce an estimate for  $\beta_0$  by approximating the space-time surface as Robertson-Walker cosmology expected to be a good approximation near the passive light-like boundary of CD. The resulting formula is tested for planetary system and Earth. The dark matter assignable to Earth can be identified as the innermost part of inner core with volume, which is .01 per cent of the volume of Earth. Also the consistency of the Bohr quantization for dark and ordinary matter is discussed and leads to a number theoretical condition on the ratio of the ordinary and dark masses.

$\beta_0/4\pi$  is analogous to gravitational fine structure constant for  $h_{eff} = h_{gr}$ . Could one see it as fundamental coupling parameter appearing also in other interactions at quantum criticality in which ordinary perturbation series diverges? Remarkably, the value of  $G$  does not appear at all in the perturbative expansion in this region! Could  $G$  have several values? This suggests the generalization  $G = l_P^2/\hbar \rightarrow G = R^2/\hbar_{eff}$  so that  $G$  would indeed have a spectrum and that Planck length  $l_P$  would be equal to  $CP_2$  radius  $R$  so that only one fundamental length would be associated with twistorialization. Ordinary Newton's constant would be given by  $G = R^2/h_{eff}$  with  $h_{eff}/h_0$  having value in the range  $10^7 - 10^8$ .

The second topic of the chapter relates to the the fact that the measurements of  $G$  give differing results with differences between measurements larger than the measurement accuracy. This suggests

that there might be some new physics involved. In TGD framework the hierarchy of Planck constants  $\hbar_{\text{eff}} = n\hbar_0$ ,  $\hbar = 6\hbar_0$  together with the condition that theory contains  $CP_2$  size scale  $R$  as only fundamental length scale, suggest the possibility that Newton's constant is given by  $G = R^2 / \hbar_{\text{eff}}$ , where  $R$  replaces Planck length ( $l_P = \sqrt{\hbar G} \rightarrow l_P = R$ ) and  $\hbar_{\text{eff}} / \hbar$  is in the range  $10^6 - 10^7$ . The spectrum of Newton's constant is consistent with Newton's equations if the scaling of  $\hbar_{\text{eff}}$  inducing scaling  $G$  is accompanied by opposite scaling of  $M^4$  coordinates in  $M^4 \times CP_2$ : dark matter hierarchy would correspond to discrete hierarchy of scales given by breaking of scale invariance. In the special case  $\hbar_{\text{eff}} = \hbar_{\text{gr}} = G M m / v_0$  quantum critical dynamics as gravitational fine structure constant  $(v_0/c)/4\pi$  as coupling constant and it has no dependence of the value of  $G$  or masses  $M$  and  $m$ .

In this chapter I consider a possible interpretation for the finding of a Chinese research group measuring two different values of  $G$  differing by 47 ppm in terms of varying  $\hbar_{\text{eff}}$ . Also a model for fountain effect of superfluidity as de-localization of wave function and increase of the maximal height of vertical orbit due to the change of the gravitational acceleration  $g$  at surface of Earth induced by a change of  $\hbar_{\text{eff}}$  due to super-fluidity is discussed. Also Podkletnov effect is considered. TGD inspired theory of consciousness allows to speculate about levitation experiences possibly induced by the modification of  $G_{\text{eff}}$  at the flux tubes for some part of the magnetic body accompanying biological body in TGD based quantum biology.