

## $M^8 - H$ duality

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1. derives from  $E^8 - E^4 \times CP_2$  duality for 4-D surfaces of octonionic space stating that if one has an associative/quaternionic 4-surface  $X^4$  in  $E^8$ , one can map it to a surface of  $E^4 \times CP_2$  by assigning to a point of  $X^4 \subset E^8$  a point  $(e_1, s)$  of  $E^4 \times CP_2$ , where  $s$  is the point of  $CP_2$  characterizing the 4 tangent plane of  $X^4$  and  $e_1$  is obtained by projecting the point  $e$  of  $E^8$  to the 4D tangent space of  $E^8$ . No  $E^8 = E^4 \times E^4$  decomposition is needed as believed originally.
2. is obtained by replacing octonions  $O$  with complexified octonions having interpretation as complexified tangent space of Minkowski space  $M^8$  and states that if one has an associative/quaternionic 4-surface  $X^4$  in  $M^8$  one can map it to a surface of  $M^4 \times CP_2$  by assigning to a point  $m_1$  of  $X^4 \subset M^8$  a point  $(m_1, s)$  of  $M^4 \times CP_2$ , where
  - (a)  $m_1$  is projection of  $m_1$  to the tangent space  $M^4 \subset M^8$  of  $X^4$ . This makes the map unique.
  - (b)  $s$  is the point of  $CP_2$  characterizing the 4 tangent plane of  $X^4$  at  $m_1$ .
3. generalizes to coassociative/coquaternionic context which is nice since both associativity and coassociativity are needed in TGD.
4. inspires the conjectures that
  - (a) the image of associative surface of  $M^8$  is associative surface in  $H$  (this need not be true).
  - (b) associative and coassociative surfaces are preferred extremals of Kähler action.
5. involves also commutativity and cocommutativity. commutative and cocommutative 2 surfaces or space time surface in  $X^4 \subset M^8$  would correspond to string world sheets and partonic 2surfaces in  $X^4 \subset H$  emerging naturally from welldefinedness of electromagnetic charge for the modes of Kähler-Dirac action and from strong form of holography.